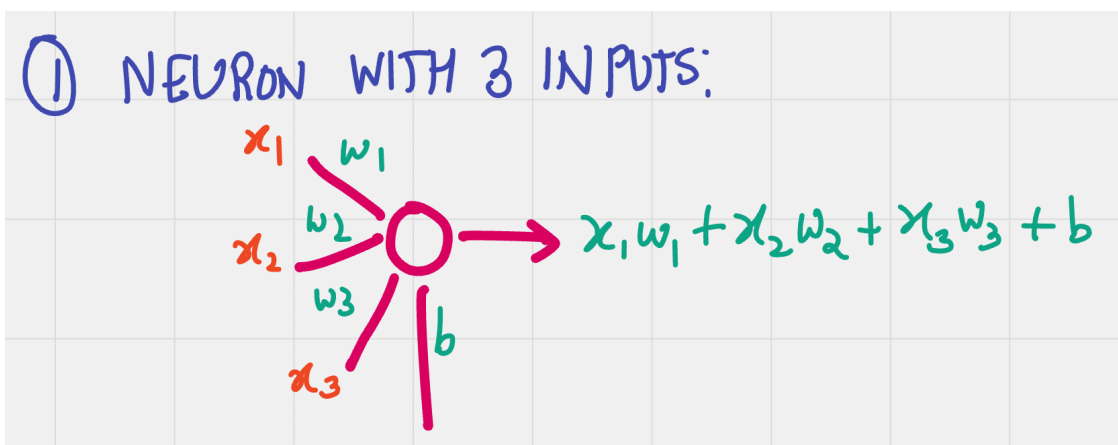


handout

October 14, 2024

0.1 BUILDING NEURAL NETWORKS FROM SCRATCH PART 1: CODING NEURONS AND LAYERS

CODING OUR FIRST NEURON: 3 INPUTS



```
[46]: inputs = [1, 2, 3]
      weights = [0.2, 0.8, -0.5]
      bias = 2

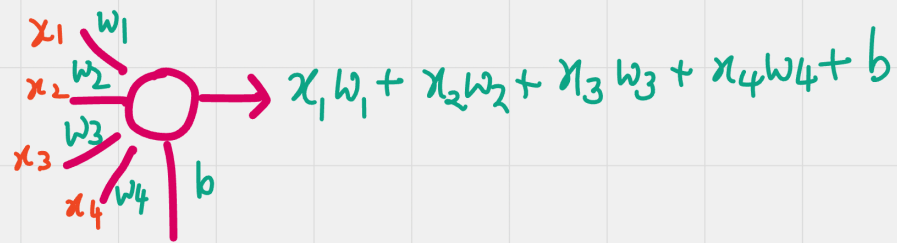
      outputs = (inputs[0]*weights[0] + inputs[1]*weights[1] + inputs[2]*weights[2] +
      ↪ bias)

      print(outputs)
```

2.3

CODING OUR SECOND NEURON: 4 INPUTS

② NEURON WITH 4 INPUTS



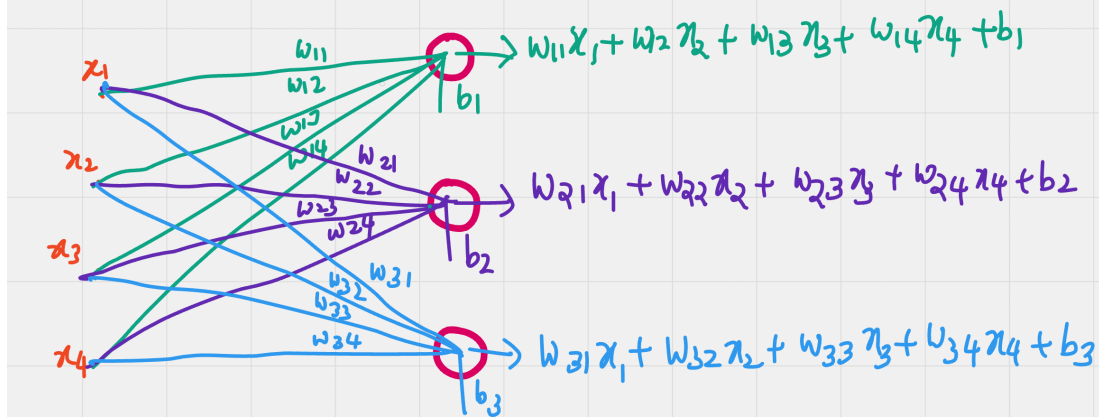
```
[47]: inputs = [1.0, 2.0, 3.0, 2.5]
weights = [0.2, 0.8, -0.5, 1.0]
bias = 2.0
output = (inputs[0]*weights[0] +
inputs[1]*weights[1] +
inputs[2]*weights[2] +
inputs[3]*weights[3] + bias)

print(output)
```

4.8

CODING OUR FIRST LAYER

③ LAYER OF NEURONS



```
[1]: inputs = [1, 2, 3, 2.5]

weights = [[0.2, 0.8, -0.5, 1],
[0.5, -0.91, 0.26, -0.5],
```

```

[-0.26, -0.27, 0.17, 0.87]]

weights1 = weights[0] #LIST OF WEIGHTS ASSOCIATED WITH 1ST NEURON : W11, W12, W13, W14
weights2 = weights[1] #LIST OF WEIGHTS ASSOCIATED WITH 2ND NEURON : W21, W22, W23, W24
weights3 = weights[2] #LIST OF WEIGHTS ASSOCIATED WITH 3RD NEURON : W31, W32, W33, W34

biases = [2, 3, 0.5]

bias1 = 2
bias2 = 3
bias3 = 0.5

outputs = [
    # Neuron 1:
    inputs[0]*weights1[0] +
    inputs[1]*weights1[1] +
    inputs[2]*weights1[2] +
    inputs[3]*weights1[3] + bias1,
    # Neuron 2:
    inputs[0]*weights2[0] +
    inputs[1]*weights2[1] +
    inputs[2]*weights2[2] +
    inputs[3]*weights2[3] + bias2,
    # Neuron 3:
    inputs[0]*weights3[0] +
    inputs[1]*weights3[1] +
    inputs[2]*weights3[2] +
    inputs[3]*weights3[3] + bias3]

print(outputs)

```

[4.8, 1.21, 2.385]

USING LOOPS FOR BETTER AND EASIER CODING

```

[50]: inputs = [1, 2, 3, 2.5]

##LIST OF WEIGHTS
weights = [[0.2, 0.8, -0.5, 1],
           [0.5, -0.91, 0.26, -0.5],
           [-0.26, -0.27, 0.17, 0.87]]

##LIST OF BIASES
biases = [2, 3, 0.5]

```

```

# Output of current layer
layer_outputs = []

# For each neuron
for neuron_weights, neuron_bias in zip(weights, biases):
    # Zeroed output of given neuron
    neuron_output = 0
    # For each input and weight to the neuron
    for n_input, weight in zip(inputs, neuron_weights):
        # Multiply this input by associated weight
        # and add to the neuron's output variable
        neuron_output += n_input*weight ##  $W_{31} \times X_1 + W_{32} \times X_2 + W_{33} \times X_3 + W_{34} \times X_4$ 
    # Add bias
    neuron_output += neuron_bias ##  $W_{31} \times X_1 + W_{32} \times X_2 + W_{33} \times X_3 + W_{34} \times X_4 + B_3$ 
    # Put neuron's result to the layer's output list
    layer_outputs.append(neuron_output)
print(layer_outputs)

```

[4.8, 1.21, 2.385]

USING NUMPY

SINGLE NEURON USING NUMPY

$$\begin{aligned}
 &\text{Inputs} = [1.0, 2.0, 3.0, 2.5] \quad \text{Bias} = 2.0 \\
 &\text{Weights} = [0.2, 0.8, -0.5, 1.0] \\
 &\text{np.dot}(\text{Weights}, \text{Inputs}) = \underbrace{1.0}_{x_1} \underbrace{(0.2)}_{w_1} + \underbrace{2.0}_{x_2} \underbrace{(0.8)}_{w_2} + \underbrace{3.0}_{x_3} \underbrace{(-0.5)}_{w_3} + \underbrace{2.5}_{x_4} \underbrace{(1.0)}_{w_4} \\
 &\quad = 2.8 \\
 &\text{bias} = 2.0 \\
 &\quad (b) \\
 &\text{np.dot}(\text{Weights}, \text{Inputs}) + \text{bias} = x_1 w_1 + x_2 w_2 + x_3 w_3 + x_4 w_4 + b
 \end{aligned}$$

```

[42]: import numpy as np
inputs = [1.0, 2.0, 3.0, 2.5]
weights = [0.2, 0.8, -0.5, 1.0]
bias = 2.0
outputs = np.dot(weights, inputs) + bias
print(outputs)

```

4.8

LAYER OF NEURONS USING NUMPY

Handwritten derivation of a neural network layer output using NumPy:

$$\text{inputs} = [1.0, 2.0, 3.0, 2.5]$$

$$\text{weights} = \begin{bmatrix} 0.2 & 0.8 & -0.5 & 1.0 \\ 0.5 & -0.91 & 0.26 & -0.5 \\ -0.26 & -0.27 & 0.17 & 0.87 \end{bmatrix}$$

$$\text{bias} = [2.0, 3.0, 0.5]$$

$$\text{np.dot}(\text{weights}, \text{inputs}) = \begin{bmatrix} \text{np.dot}(\text{weights}[0], \text{inputs}), \\ \text{np.dot}(\text{weights}[1], \text{inputs}), \\ \text{np.dot}(\text{weights}[2], \text{inputs}) \end{bmatrix}$$

Diagram illustrating the output calculation:

- x_1 : $\text{np.dot}(\text{weights}[0], \text{inputs}) + \text{bias}[0]$
- x_2 : $\text{np.dot}(\text{weights}[1], \text{inputs}) + \text{bias}[1]$
- x_3 : $\text{np.dot}(\text{weights}[2], \text{inputs}) + \text{bias}[2]$

[43]: *## In plain Python, we wrote this as a list of lists. With NumPy, this will be a 2-dimensional array, which we'll call a matrix.*

[44]:

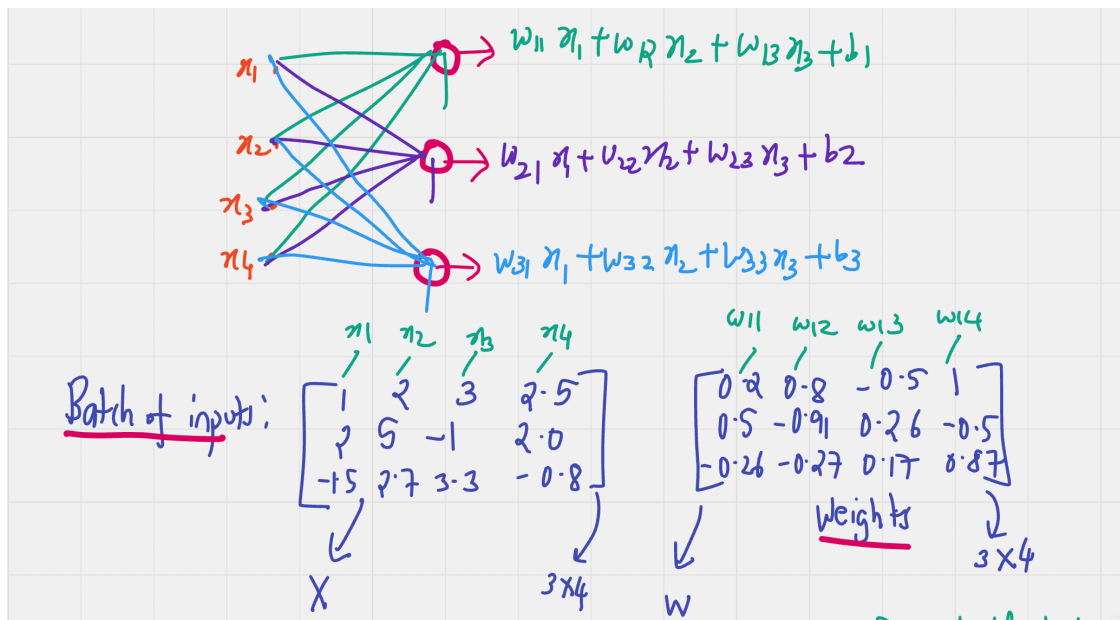
```
inputs = [1.0, 2.0, 3.0, 2.5]
weights = [[0.2, 0.8, -0.5, 1],
            [0.5, -0.91, 0.26, -0.5],
            [-0.26, -0.27, 0.17, 0.87]]
biases = [2.0, 3.0, 0.5]

# A dot product of a matrix and a vector results in a list of dot products.
# The np.dot() method treats the matrix as a list of vectors and performs a dot
# product of each of those vectors with the other vector

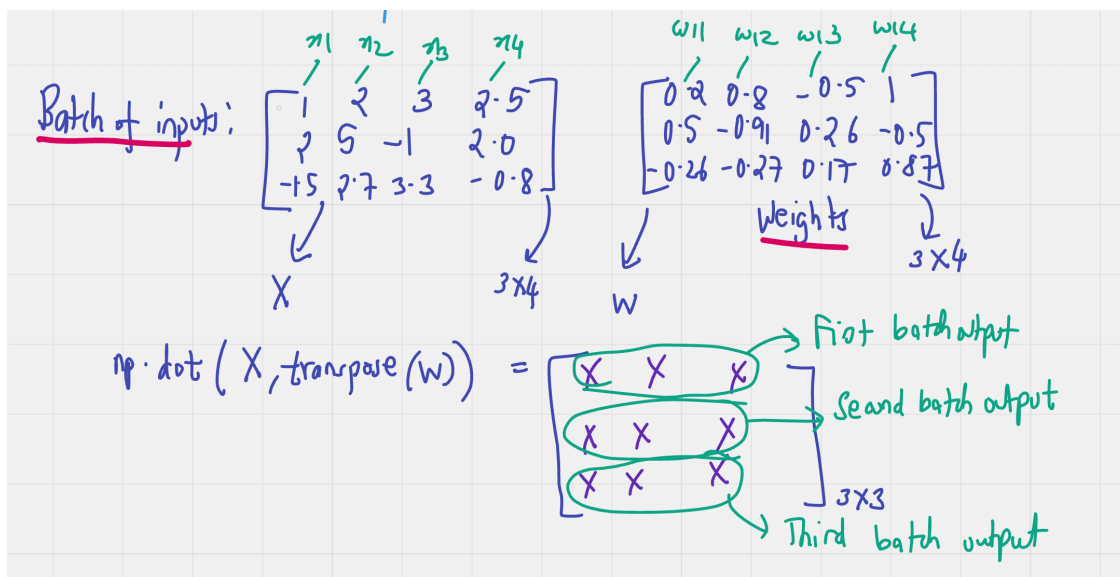
layer_outputs = np.dot(weights, inputs) + biases
print(layer_outputs)
```

[4.8 1.21 2.385]

LAYER OF NEURONS AND BATCH OF DATA USING NUMPY



NEED TO TAKE TRANSPOSE OF WEIGHT MATRIX



```
[45]: inputs = [[1.0, 2.0, 3.0, 2.5], [2.0, 5.0, -1.0, 2.0], [-1.5, 2.7, 3.3, -0.8]]
weights = [[0.2, 0.8, -0.5, 1],
           [0.5, -0.91, 0.26, -0.5],
           [-0.26, -0.27, 0.17, 0.87]]
biases = [2.0, 3.0, 0.5]

# NOTE: WE CAN'T TRANSPOSE LISTS IN PYTHON, SO WE HAVE TO CONVERT THE WEIGHTS
# MATRIX INTO AN ARRAY FIRST
outputs = np.dot(inputs, np.array(weights).T) + biases
print(outputs)
```

```
[[ 4.8    1.21   2.385]
 [ 8.9   -1.81   0.2  ]
 [ 1.41   1.051  0.026]]
```

```
[ ]:
```